15EE54

Fifth Semester B.E. Degree Examination, Feb./Mar. 2022 Signals and Systems

Time: 3 hrs.

Max. Marks: 80

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- a. Explain the following classes of signals
 - i) Periodic an Non-periodic signals

ii) Energy and power signals

(04 Marks)

b. Find the even and odd parts of the signal x(t) shown in Fig Q1(b).

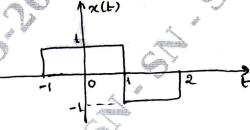


Fig Q1(b)

(04 Marks)

c. Sketch the waveforms for the following signals:

i)
$$x_1(t) = u(t+2) - 2u(t) + u(t-2)$$

ii)
$$x_2(t) = -u(t+3) + 2u(t+1) - 2u(t-1) + u(t-3)$$

iii) $x_3(t) = r(t+1) - r(t) + r(t-2)$

iv)
$$x_4(t) = r(t+2) - r(t+1) - r(t-1) + r(t-2)$$

(08 Marks)

OR

- 2 a. Determine the average power and the energy of the following sequences:
 - i) $x_1(n) = nu(n)$
 - ii) $x_2(n) = A_0 e^{J\Omega_0 n}$

(06 Marks)

- b. Determine whether the system described by, $y(t) = e^{x(t)}$ is:
 - i) Linear
 - ii) Time invariant
 - iii) Stable.

(06 Marks)

c. A discrete time system is represented by the following input output relation: y(n) = 2x(n) + 3x(n-1) + 4x(n-2) + 5x(n-3). Draw the block diagram showing the parallel implementation of system operator 'H'. (04 Marks)

Module-2

3 a. Find the convolution of the two discrete sequence given below:

$$x_1(n) = 2^n u(-n-1)$$

 $x_2(n) = 4^n u(-n-1)$

8

(08 Marks)

b. Evaluate the step response for the LTI system represented by the impulse response,

t) = $e^{-|t|}$.

(04 Marks)

- c. Determine whether the system described by its impulse response $h(n) = e^{2n} u (n-1)$ is
 - i) Causal

ii) Stable.

(04 Marks)

OR

- 4 a. Find the response of the system described by the difference equation $y(n) + 4y(n-1) + 4y(n-2) = 2^n u(n)$ with y(-1) = 0, y(-2) = 1. (08 Marks)
 - Draw the direct form I and direct form II implementation for the system described by the differential equation $\frac{d^3y(t)}{dt^3} + 2\frac{dy(t)}{dt} + 3y(t) = x(t) + 3\frac{dx(t)}{dt}.$ (08 Marks)

Module-3

- 5 a. State and prove duality property of continuous time Fourier transformer. (04 Marks)
 - b. Find the Fourier transform of a rectangular pulse described below:

$$x(t) = \begin{cases} 1, & |t| < a \\ 0, & |t| > a \end{cases}$$
. Also sketch the magnitude and phase spectra. (08 Marks)

c. Find the inverse Fourier transform of x(jw) for the spectra shown in Fig Q5(c) i) and Fig Q5(c) ii) below:

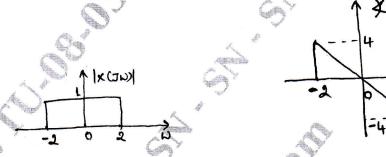


Fig Q5(c) i) #

Fig Q5(c) ii) (04 Marks)

OR

- 6 a. Determine the frequency response of the system described by the impulse response, $h(t) = \delta(t) 2e^{-2t}u(t)$. Also sketch the spectra. (06 Marks)
 - b. Find the frequency response and the impulse response of the system described by the differential equation:

$$\frac{d^2y(t)}{dt^2} + 3\frac{dy(t)}{dt} + 2y(t) = x(t).$$
 What is the response of the system is $x(t) = t e^{-t}u(t)$?
(10 Marks)

Module-4

- 7 a. State and prove summation property of discrete time Fourier transforms. (05 Marks)
 - b. Compute the DTFT of the signal, $x(n) = \cos\left(0.2n\pi + \frac{\pi}{4}\right)$ and sketch the amplitude and phase spectra over $-\pi \le \Omega \le \pi$. (07 Marks)
 - c. Find the inverse DTFT of $x(e^{j\Omega}) = e^{-j4\Omega}$, $\frac{\pi}{2} < |\Omega| < \pi$ (04 Marks)

OR

8 a. Determine the frequency response and the impulse response of the system described by the difference equation $y(n) - \frac{1}{2}y(n-1) = x(n) + \frac{1}{2}x(n-1)$. What is the response of the system

to an input
$$x(n) = Cos\left(\frac{\pi}{2}n\right)$$
 (08 Marks)